The Skyscraper Problem: Quadratic Solution

Finding a

$$19 = 2a$$
$$a = 9.5$$

Now we have
$$y = 9.5x^2 + bx + c$$

Finding c

The cost of 0 floors is 0 dollars, so the y-intercept, c, is 0.

Now we have
$$y = 9.5x^2 + bx + 0$$

Finding b

Substitute the known point (2, 171) into the equation.

$$171 = 9.5(2^2) + b(2)$$

$$171 = 38 + 2b$$

$$\frac{133}{2} = \frac{2b}{2}$$

$$66.5 = b$$

Which leaves us with $y = 9.5x^2 + 66.5x$, or, in the context of this situation, $f(n) = 9.5n^2 + 66.5n$